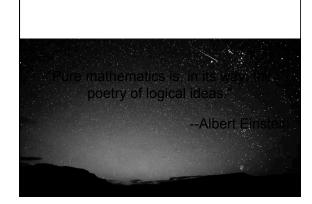
Math Learning Disabilities,
Dyslexia and ADHD:
Understanding and Remediating MLD
Diana Kennedy, MA, BCET

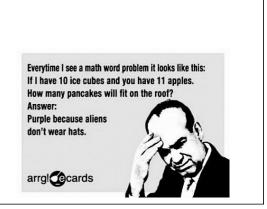


# Proud member of The Association of Educational Therapists

The Association of Educational Therapists is the national professional association for educational therapists. AET defines and sets standards for the professional practice of educational therapy. Educational therapists provide a broad range of individualized educational interventions for children and adults with learning disabilities and other learning challenges.

https://www.aetonline.org/





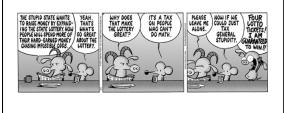
#### **Prevalence**

- Math difficulties ~ 35%
- Math disability ~ 6.4%
- As common as Dyslexia and ADHD
- Familial prevalence 10X general population



(Shalev, 52; Gersten, Clarke, and Mazzocco, 13 in Berch & Mazzocco (Eds). 2009.)

#### The "So What?"



The "So What?"	,
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ROYALE	RASMUSSEN REPORTS POLL Did scientists falsify research to support their own theories on Global Warming?
VIDEO POKER	59% SOMEWHAT LIKELY 35% VERY LIKELY 26% NOT VERY LIKELY
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# **Agenda**

- What is a math learning disability (MLD)?
  - Connections to Dyslexia & ADHD.
- · What to do about it?

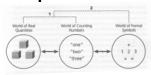


# Agenda

- What is a math learning disability (MLD)?
  - Connections to Dyslexia & ADHD.
- · What to do about it?



# **Math Competence**



"Math competence rests, fundamentally, on the construction of a rich set of conceptual relationships among these worlds."

(Griffin, 375-376 in Berch & Mazzocco, (Eds). 2009.)

# **Math Competence**

Procedural knowledge

Conceptual

Factual knowledge

"The cooperation of [these] different types of knowledge leads to meaningful and efficient processing."

(Zamarian, López-Rolón, & Delazer, 260 in Berch & Mazzocco, (Eds). 2009.)

#### **Definitions of MLD**

"Dyscalculia can best be defined as a deficit in the **representation or processing** of specifically numerical information."

quoting Landerl et al. (Jordan, 111 in Berch & Mazzocco, (Eds). 2009.)

#### **Definitions of MLD**

which "affects the ability to acquire mathematical skills despite appropriate instruction."

(Chinn & Ashcroft, 13)

(Gersten, Clarke, and Mazzocco, 22 in Berch & Mazzocco, (Eds). 2009.)

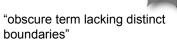
# **Definitions of MLD**

#### DSM-V:

- Specific Learning Disorder with impairment in math
  - number sense
  - memorization of arithmetic facts
  - accurate or fluent calculation
  - accurate math reasoning

#### **Definitions of MLD**

- · No biological markers
- · No qualitative markers



(Berch & Mazzocco, (Eds). 2009.)

5

Coo	initive	processes	in	math
~~~		DI COCCOCO		HILLAGE

- Domain general (Geary)
- Domain specific (Butterworth)
- basic processes
- hard-wiring for math
- underlie many tasks
- "number module"
- ~ overlaps with other LDs
- ~ MLD

(Jordan in Berch & Mazzocco, (Eds). 2009.)

#### **Domain General Problems**

- · Language processing
  - Dyslexia or other language-based difficulties
  - Difficulties with information representation and manipulation in the language system
  - Deficit in the ability to retrieve facts from a semantics-based long-term memory network

(Gersten, Clarke, and Mazzocco, 19 in Berch & Mazzocco, (Eds). 2009.)

# **Dyslexia and MLD**

- 70-80% of kids with Dyslexia have MLD
- 50-66% of kids with MLD have Dyslexia



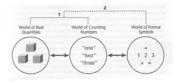


(Dolan, 168 & Jordan, 106 & Shalev, 54 in Berch & Mazzocco, (Eds). 2009.)

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# **Dyslexia and MLD**

- 70-80% of kids with Dyslexia have MLD
- 50-66% of kids with MLD have Dyslexia



# **Dyslexia and MLD**

- · Language center's contribution to MLD
  - representing and manipulating verbal information
  - retrieving facts from semantics-based long-term memory
  - verbal mediation



# **Dyslexia and MLD**

- MLD with Dyslexia or other languagebased difficulties more severe than MLD alone
- May have trouble using language as a compensatory strategy (verbal mediation)

_				
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- · Students with language impairments need
  - Explicit instruction in language of math
    - "Shaded in"
    - Multiple ways to say same concept

15÷3





**Domain General Problems** 

- · Working memory impairments
  - Often in both Dyslexia & ADHD
  - Memorizing facts
  - Procedural breakdowns



(Geary, Hoard, Nugent, Byrd-Craven, 92 in Berch & Mazzocco, (Eds). 2009.)

#### **Domain General Problems**

- · Memorizing facts
  - to learn math facts, parts of equation and answer must both be simultaneously active in the phonological buffer (loop).



- · Memorizing facts
  - Inefficient and inaccurate retrieval of math facts one of the hallmarks of MLD
  - Domino effect on rest of math
  - Takes up precious processing power





#### **Domain General Problems**

- · Memorizing facts
  - Need facts taught explicitly
  - May not make connections on their own
  - Give visual strategies
    - 100's chart
    - number line
    - blocks





#### **Domain General Problems**

- · Procedural Breakdowns
  - How many steps?

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(Zentall, 221 in Berch & Mazzocco, (Eds). 2009.)

- · Procedural breakdowns
  - Exacerbated by lack of automaticity
  - Processing resources filled by inefficient fact recall
  - Takes away from more complex processing



(Bull, summary, 289 in Berch & Mazzocco, (Eds). 2009

#### **Domain General Problems**

- · Procedural breakdowns
  - Accommodations for math facts (off-load processing)
  - Mnemonic or checklist for order of procedures
  - Sample problems"No offense, but I don't listen..."



(Bull, summary, 289 in Berch & Mazzocco, (Eds). 2009.

#### **Domain General Problems**

- · Processing Speed
  - Often part of Dyslexia and ADHD
  - Affects decay rate in phonological loop
  - Teachers use speed as proxy for automaticity
  - For kids w/slow processing, not a good proxy



(Geary, Hoard, Nugent, Byrd-Craven, 93 in Berch & Mazzocco, (Eds). 2009.)

- · Central executive
  - Main weakness in ADHD
  - Poor inhibition of irrelevant associations



(Geary, Hoard, Nugent, Byrd-Craven, 92 in Berch & Mazzocco, (Eds). 2009

#### **Domain General Problems**

- · Central executive
  - Main weakness in ADHD
  - Poor inhibition of irrelevant associations
  - Attention control



(Geary, Hoard, Nugent, Byrd-Craven, 92 in Berch & Mazzocco, (Eds). 2009.)

#### **Domain General Problems**

- · Central executive
  - Main weakness in ADHD
  - Poor inhibition of irrelevant associations
  - Attention control
  - Clutters WM and further limits it



(Geary, Hoard, Nugent, Byrd-Craven, 93 in Berch & Mazzocco, (Eds). 2009.

#### **ADHD** and **MLD**

- 31% of kids with ADHD have MLD
- 25% of kids with MLD have ADHD





(Zentall, 220 & Shalev in Berch & Mazzocco, (Eds). 2009.)

#### **ADHD** and **MLD**

- Generally NOT an issue of conceptual understanding
- Biggest challenge is in memorizing and recalling math facts
- · ADHD brain has weak executive functions

(Zentall, 221 in Berch & Mazzocco, (Eds). 2009.)

#### **ADHD** and **MLD**

- ADHD brain habituates to stimuli very fast
  - Difficult to maintain attention to repetitive stimulus
    - · Spend less time rehearsing
    - More errors, especially during later trails of rote or overly familiar tasks

(Zentall, 221 in Berch & Mazzocco, (Eds). 2009.)

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ı	•

# **ADHD** and **MLD**

- · Detail analysis
  - Signs, operations, exponents

 $-4^2 + (-5^2) \div 7$ 

(Zentall, 227 in Berch & Mazzocco, (Eds). 2009.)

#### **ADHD** and **MLD**

- ADHD brain low frustration tolerance
  - Pushing through difficult problems
  - Self-image more affected by mistakes



(Zentall, in Berch & Mazzocco, (Eds). 2009.)

#### **ADHD** and **MLD**

- · ADHD brain helped by
  - color-coding

-42 + (-52) ÷7

- games
  - with public acknowledgement
  - · on a computer
- Learning self-monitoring and goal setting
  - · charting progress

(Pickering & Gathercole, 2004 quoted inZentall, 22 in Berch & Mazzocco, (Eds). 2009.)

#### **ADHD** and **MLD**

- · ADHD brain helped by
  - Verbalizing problems
  - Sorting types of word problems
  - Music, Gum, Bouncy-ball,
     Utzie cushion (stimulation)



(Pickering & Gathercole, 2004 quoted inZentall, 22 in Berch & Mazzocco, (Eds). 2009.)

#### **ADHD** and **MLD**

- · ADHD brain helped by
  - stimulant medicine increases
    - number of attempted problems
    - number of responses correct
    - number of responses correct per minute
    - number of self-corrected errors

(Zentall, 231 in Berch & Mazzocco, (Eds). 2009.)

#### **Domain General Problems**



- Visuospatial representations
  - · May contribute to Dyslexia or stand alone
  - Weakness in representations of number magnitude
  - influences early acquisition of calculation

3 + 1 = 4

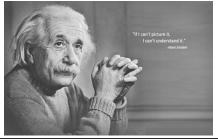
may underpin retrieval

difficulties

0 1 2 3 4 5 6 7 8 9 10

(Bull, summary, 266 in Berch & Mazzocco (Eds). 2009.)

# **Domain General Problems**

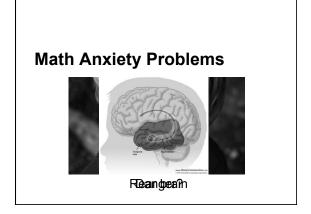


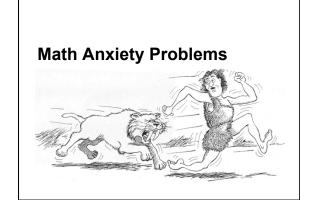
# **Math Anxiety Problems**



The amygdala: traffic cop of the brain Where do signals go?

# Math Anxiety Problems Prefrontal Cortex Ventromedial perfontal cortex Amygdala Frontitalase fitex





# **Math Anxiety Problems**

The only problem is that the amygdala cannot tell the difference between...



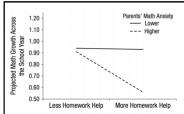


# **Math Anxiety Problems**

"[W]hen parents frequently help their children with math homework, increased math anxiety in the parents leads to decreased end-of-year math achievement in their children."

Maloney et al (2015) Intergenerational effects

# **Math Anxiety Problems**



Maloney et al (2015) Intergenerational effects

# **Math Anxiety Problems**

- · Anxious kids need
  - Growth mindset
    - Jo Boaler: youcubed https://www.youcubed.org/



- Games
  - · laughter is the anti-stress



# **Domain Specific Problems**

- Number module
  - for detecting, comparing, manipulating 'numerosity parameter'



- system for representing & retrieving arithmetical knowledge
- Parietal lobes

(Butterworth and Reigosa in Berch & Mazzocco, (Eds). 2009.)

# **Domain Specific Problems**

· Number module

Number Module: Approximate number; allows for estimation --Nonverbal, nonsymbolic

Verbal System: Exact number; words allow representation, memory & calculation of exact numbers

Verbal, symbolic

(Zamarian, López-Rolón, & Delazer, 258 in Berch & Mazzocco, (Eds). 2009.)

# **Domain Specific Problems**

Number module
 Poor subitizing



(Gersten, Clarke, and Mazzocco, 20; Jordan in Berch & Mazzocco (Eds). 2009.)

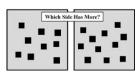
# **Domain Specific Problems**

Subitizing: Rainman

(Gersten, Clarke, and Mazzocco, 20; Jordan in Berch & Mazzocco (Eds). 2009.)

# **Domain Specific**

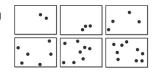
- · Number module
  - Poor comparison of amounts



(Illustration David Mills, Dyscalculia http://mathdifficulties.blogspot.com/) (Gersten, Clarke, and Mazzocco, 20; Jordan in Berch & Mazzocco (Eds). 2009.)

# **Domain Specific**

- Number module
  - Poor sequencing of amounts



(Illustration http://daily.zhihu.com/story/4066465)

(Gersten, Clarke, and Mazzocco, 20; Jordan in Berch & Mazzocco (Eds). 2009.)

# **Agenda**

- What is a math learning disability (MLD)?
  - Connections to Dyslexia & ADHD.
- · What to do about it?



#### What to do about an MLD?

- Concept-procedure integration
- · Explicit, explicit, explicit
- · Increment, increment, increment
- Games
- Accommodations

# **Concept-procedure integration**

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# **Concept-procedure integration**

"Math wars"

• Not either / or Procedural knowledge

 Need to bridge all three

Language as the bridge

Conceptual knowledge
Knowledge
Knowledge

David Berg, Making Math Real™ http://www.makingmathreal.org/

# **Concept-procedure integration**

- · Bring out the base ten blocks!
- The missing piece: making the connection
   Concrete →

Semi-concrete→
Semi-abstract→
Abstract



David Berg, Making Math Real™ http://www.makingmathreal.org/

# **Concept-procedure integration**

- Concrete = Manipulatives
- Record (color-coded) what the manipulatives demonstrate





David Berg, Making Math Real™ http://www.makingmathreal.org/

# **Concept-procedure integration**

- Make explicit that manipulatives and symbols "Tell the same story."
- · Language becomes the bridge





David Berg, Making Math Real™ http://www.makingmathreal.org/

# **Concept-procedure integration**

- · Semi-concrete
  - Part I: go through the concrete steps
  - Part II: redo the problem with just the math prompts
  - To give student practice with only symbols, but with manipulatives and recording fresh in memory

David Berg, Making Math Real™ http://www.makingmathreal.org/

Concept-procedure integration	
Semi-abstract	
– Just symbols	
<ul><li>Color-coded</li><li>56</li></ul>	
+ 33 89	
David Berg, Making Math Real™ http://www.makingmathreal.org/	
Concept-procedure integration	
<ul> <li>Abstract</li> <li>Just the symbols without color-coding</li> </ul>	
<ul> <li>If student loses the picture,</li> </ul>	
go back to earlier stage  – This is where most textbooks 56	
and worksheets start + 33	
89	
David Berg, Making Math Real™ http://www.makingmathreal.org/	

# Explicit, explicit!

- Facts
- Problem solving strategies
- Self-monitoring
- · Checking work
- · Using accommodations
- Anything else you can think of!

# **Explicit, explicit, explicit!**

- · Problem solving strategies
  - Explicitly teach problem solving strategy
  - Once mastered, explicitly teach how to transfer to novel situations, structure
  - Explicitly teach categorization
  - Best when taught with self-regulated learning strategies

(Fuchs and Fuchs in Berch, D.B. & Mazzocco, M.M. (Eds). 2009.)

# Increment, increment, increment

- · Task analysis
  - How many new concepts are introduced between the first and the second problem?

243 803 +415 +419

# Increment, increment, increment

- · Task analysis
  - Understand which changes represent a new concept
  - Explicitly teach one new concept at a time
  - New concept, old content; new content, old concept
  - If kids are confused, break it down further

 -	•	

## **Games**

- · Why games?
  - ADHD attention
  - Anxiety and laughter
  - Makes overlearning fun
  - "Need to know"



#### **Games**

- Make sure you are targeting what you want to target
  - Simply fact memorization?
  - Concept?
  - Procedure?
  - Number sense?

#### **Games**

- General purpose
  - Problems on board with sticky ball
  - Teacher/Parent vs student
  - Sports ball
  - Game board



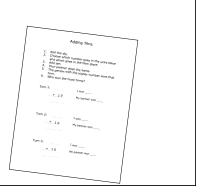
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# **Games**

- Card games
  - Go fish
  - Slap jack
  - Memory

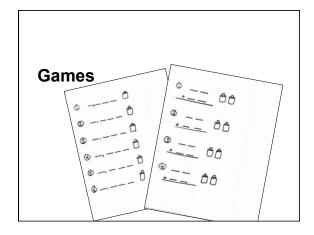


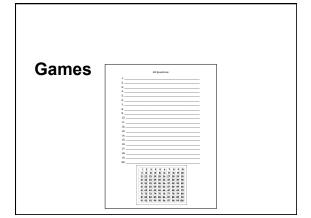
# **Games**



## **Games**







# Accommodations Assignments and tests need discrete goals Use accommodations to support non-goal tasks

#### **Accommodations**

- · Effective accommodations
  - need to be taught explicitly
  - some are disposable crutches
  - some are lifetime supports
  - integrate throughout classes & at home

#### **Accommodations**

- Extended time
- · Modified homework load (time-based versus length-based)
  - Check in with students: "Sasha"
- Number line
- Multiplication chart or nine-lines



# **Accommodations**

**FAIR** does not mean

Same







1	o
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"Mathematics is one of the essential emanations of the human spirit--a thing to be valued in and for itself, like art or poetry."



--Oswald Veblen

#### Thank You

Diana Kennedy, MA, ET/P Educational Therapist, Author, Speaker www.MindSparkLearning.com 510-610-6294 @teacherDBK to sign up for newsletter, http://eepurl.com/OflhP

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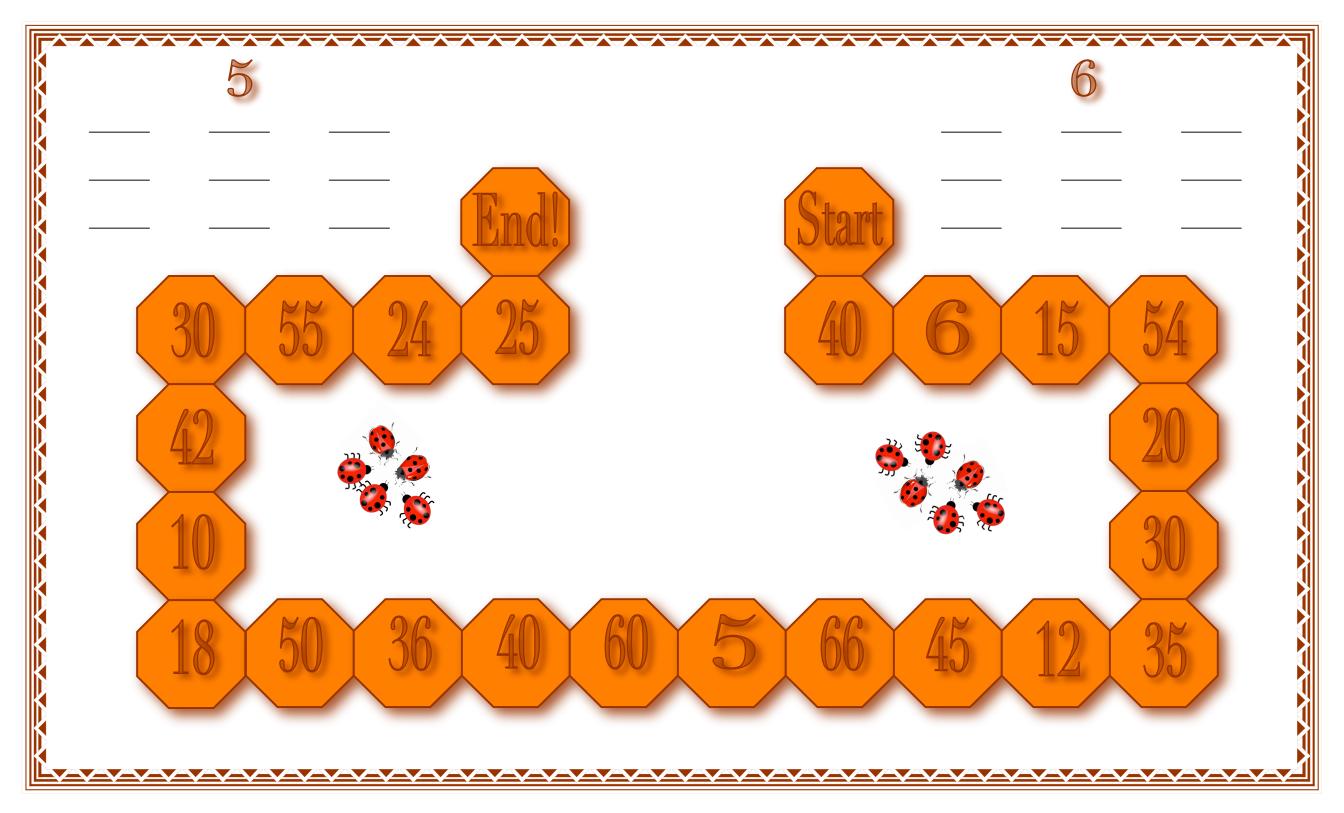
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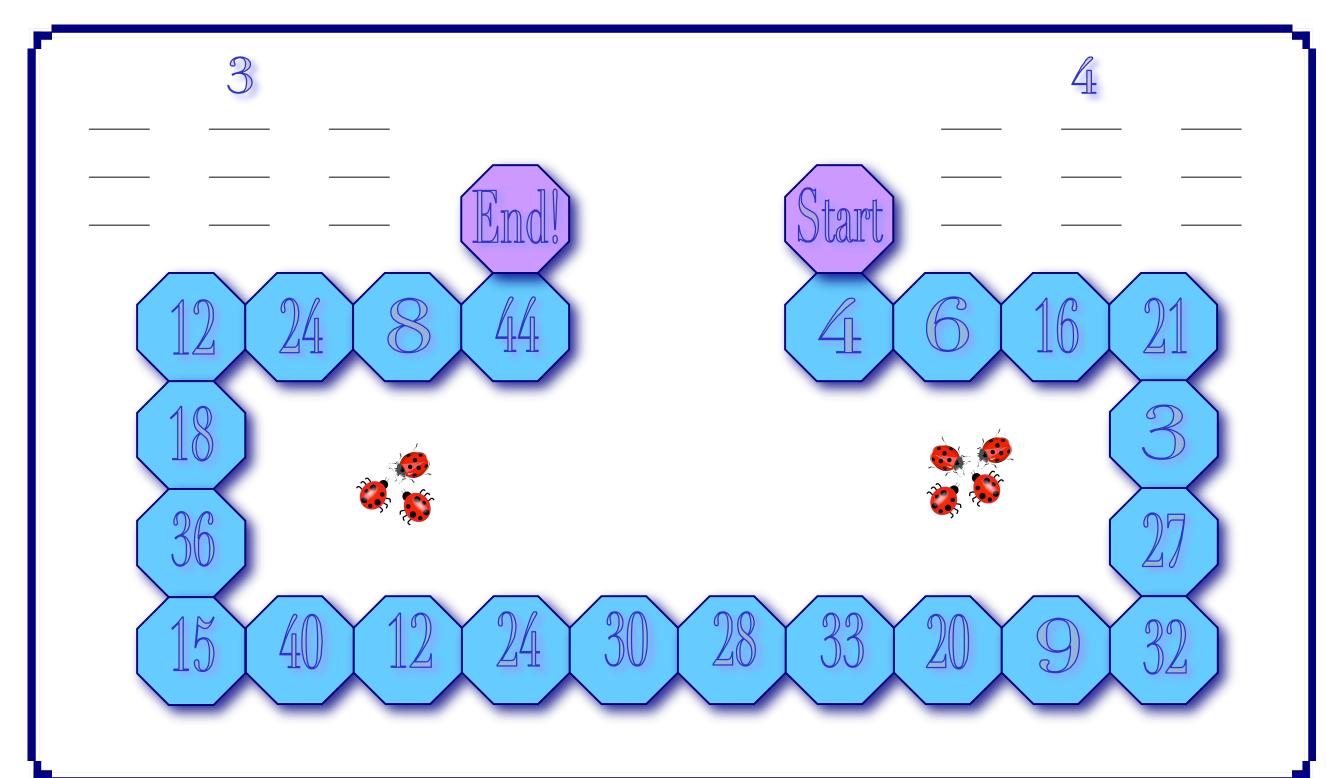
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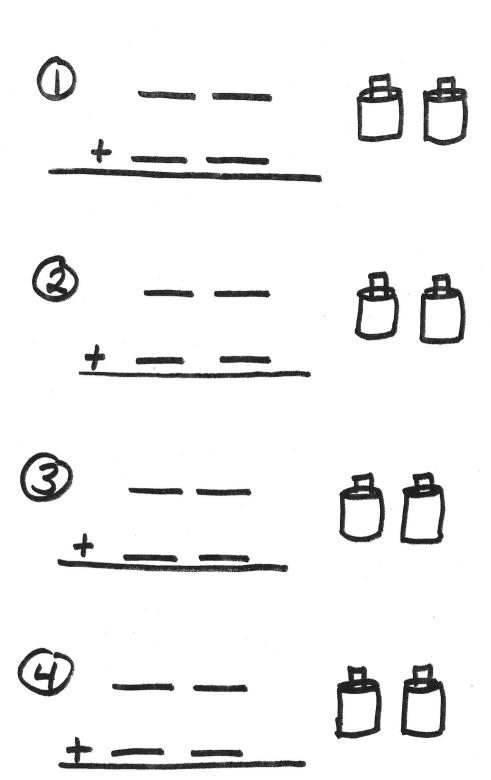
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# 20 Questions

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